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Tavan T Trent* (ttrent@as.ua.edu), Dept. of Mathematics, University of Alabama,
Tuscaloosa, AL 35487. *The Douglas Property for Multiplier Algebras.*

Let $\mathcal{H}(\Omega)$ denote a reproducing kernel Hilbert space of functions on Ω with multiplier algebra, $\mathcal{M}(\mathcal{H}(\Omega))$. An algebra, \mathcal{A} , of $B(\mathcal{H}(\Omega))$ has the *Douglas property* if whenever $A_{ij}, B_{ij} \in \mathcal{A}$ with $[A_{ij}], [B_{ij}] \in B(\bigoplus_{n=1}^{\infty} \mathcal{H}(\Omega))$ with $[A_{ij}][A_{ij}]^* \geq [B_{ij}][B_{ij}]^*$, then there exists $C_{ij} \in \mathcal{A}$ with $[C_{ij}] \in B(\bigoplus_{n=1}^{\infty} \mathcal{H}(\Omega))$ satisfying:

$$(1) \quad [A_{ij}][C_{ij}] = [B_{ij}]$$

and

$$(2) \quad \|[C_{ij}]\| \leq 1.$$

For a *nice* kernel, McCullough and I have shown

THEOREM: Assume that $\mathcal{H}(\Omega)$ is *nice*. $\mathcal{H}(\Omega)$ has an NP kernel $\iff \mathcal{M}(\mathcal{H}(\Omega))$ has the *Douglas property*. (Received June 21, 2011)