

1072-57-55

**Alexander Dranishnikov\*** ([dranish@math.ufl.edu](mailto:dranish@math.ufl.edu)), Department of Mathematics, University of Florida, Gainesville, FL 32611-8105. *Essential manifolds and macroscopic dimension.*

The following definitions are due to Gromov.

An  $n$ -manifold  $M$  is called *rationally essential* if  $im(f_*) \neq 0$  in  $H_n(B\pi; \mathbb{Q})$  where  $f : M \rightarrow B\pi$  is a map that classifies the universal covering of  $M$ .

A metric space  $X$  has the macroscopic dimension at most  $n$ ,  $\dim_{mc} X \leq n$  if there is a continuous map  $g : X \rightarrow K^n$  to an  $n$ -dimensional simplicial complex and a number  $b > 0$  such that  $diam(g^{-1}(y)) < b$  for all  $y \in K^n$ .

We present a counterexample to the following conjecture of Gromov: *For every rationally essential  $n$ -manifold  $M$  the universal covering  $\tilde{M}$  taken with the lifted metric should have the macroscopic dimension equal to  $n$ ,  $\dim_{mc} \tilde{M} = n$ .* (Received June 14, 2011)