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Marius Beceanu* (mbeceanu@math.rutgers.edu), 110 Frelinghuysen Rd., Rutgers University
Math. Dept., Piscataway, NJ 08854. *Structure of wave operators in R^d .*

We prove a structure formula for the wave operators in \mathbb{R}^3

$$W_{\pm} = \lim_{t \rightarrow \pm\infty} e^{it(-\Delta+V)} P_c e^{it\Delta}$$

and their adjoints for a scaling-invariant class of scalar potentials $V \in B$,

$$B = \left\{ V \mid \sum_{k \in \mathbb{Z}} 2^{k/2} \|\chi_{|x| \in [2^k, 2^{k+1}]}(x) V(x)\|_{L^2} < \infty \right\},$$

under the assumption that zero is neither an eigenvalue, nor a resonance for $-\Delta + V$.

The formula implies the boundedness of wave operators on L^p spaces, $1 \leq p \leq \infty$, on weighted L^p spaces, and on Sobolev spaces, as well as multilinear estimates for $e^{itH} P_c$.

When V decreases rapidly at infinity, we obtain an asymptotic expansion of the wave operators. The first term of the expansion is of order $\langle y \rangle^{-4}$, commutes with the Laplacian, and exists when $V \in \langle x \rangle^{-3/2-\epsilon} L^2$.

We also prove that the scattering operator $S = W_-^* W_+$ is an integrable combination of isometries.

The proof is based on an abstract version of Wiener's theorem, applied in a new function space. (Received July 30, 2011)