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Tutte's Linking Theorem is a generalization of Menger's Theorem from graphs to matroids. It has proven to be of great value in the study of matroid connectivity.

Let S and T be disjoint subsets of the groundset of a matroid M . The *connectivity* between S and T , denoted $\kappa_M(S, T)$, is the minimum order of a separation (X, Y) with $S \subseteq X$ and $T \subseteq Y$. Tutte's Linking Theorem states that, for all elements e outside S and T , at least one of $M \setminus e$ and M/e has the same connectivity between S and T as M .

In this talk we have two pairs of subsets, (S_1, T_1) and (S_2, T_2) , of the groundset of M . We show that, if M is sufficiently large and representable over a finite field, we can find an element e such that in one of $M \setminus e$ and M/e *both* connectivities are preserved.

We conjecture that the bound on the size of M does not depend on the field. (Received January 28, 2012)