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**Oleg Borodin** and **Alexandr Kostochka\***, kostochk@math.uiuc.edu. *Improper 2-colorings of sparse graphs*. Preliminary report.

We consider one of the simplest kinds of improper colorings – colorings with two colors. A graph  $G$  is  $(j, k)$ -colorable if its vertices can be partitioned into subsets  $V_1$  and  $V_2$  such that in  $G[V_1]$  every vertex has degree at most  $j$  and in  $G[V_2]$  every vertex has degree at most  $k$ . We prove that every graph with the maximum average degree at most  $\frac{12}{5}$  is  $(1, 0)$ -colorable and that if  $k \geq 2j + 2$ , then every graph with maximum average degree at most  $2 \left( 2 - \frac{k+2}{(j+2)(k+1)} \right)$  is  $(j, k)$ -colorable. Both bounds are sharp. (Received January 11, 2012)