

1083-05-58

**Nicholas A. Loehr, Jeffrey B. Remmel and Bruce E. Sagan\*** (sagan@math.msu.edu). *A factorization theorem for  $m$ -rook placements.* Preliminary report.

Let  $B = (b_1, b_2, \dots, b_n)$  be an integer partition where the parts are listed in weakly increasing order. We also consider  $B$  as a Ferrers board where  $b_j$  is the height of column  $j$  and the columns are bottom justified. Letting  $r_k(B)$  denote the number of placements of  $k$  rooks on any board  $B$  and  $x \downarrow_k = (x)(x-1)\cdots(x-k+1)$ , we have the famous Factorization Theorem of Goldman-Joichi-White which states that for any Ferrers board as above we have  $\sum_{k \geq 0} r_k(B) x \downarrow_{n-k} = \prod_j (x + b_j - j + 1)$ . Briggs and Remmel considered a generalization of rook placements to  $m$ -rook placements which are related to wreath products  $C_m \wr S_N$  where  $C_m$  is a cyclic group and  $S_N$  a symmetric group. Ordinary rook placements correspond to the case  $m = 1$ . They were able to prove a version of the Factorization Theorem in this setting, but only for certain Ferrers boards. We give a generalization which holds for all Ferrers boards. (Received August 14, 2012)