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**Shrawan Kumar\*** ([shrawan@email.unc.edu](mailto:shrawan@email.unc.edu)), Department of Mathematics, Chapel Hill, NC 27599-3250. *Positivity in  $T$ -Equivariant  $K$ -theory of flag varieties associated to Kac-Moody groups*. Preliminary report.

Let  $G$  be any symmetrizable Kac-Moody group completed along the negative roots and  $G^{min} \subset G$  be the ‘minimal’ Kac-Moody group. Let  $B$  be the standard (positive) Borel subgroup,  $B^-$  the standard negative Borel subgroup,  $H = B \cap B^-$  the standard maximal torus and  $W$  the Weyl group. Let  $\bar{X} = G/B$  be the ‘thick’ flag variety (introduced by Kashiwara) which contains the standard KM flag ind-variety  $X = G^{min}/B$ . Let  $T$  be the quotient torus  $H/Z(G^{min})$ , where  $Z(G^{min})$  is the center of  $G^{min}$ .

Let  $K_T^{top}(X)$  be the  $T$ -equivariant topological  $K$ -group of  $X$ . Let  $\{\psi^w\}_{w \in W}$  be the ‘basis’ of  $K_T^{top}(X)$  given by Kostant-Kumar. Express the product in  $K_T^{top}(X)$ :

$$\psi^u \cdot \psi^v = \sum_w p_{u,v}^w \psi^w, \quad \text{for } p_{u,v}^w \in R(T).$$

Then, the following result is our main theorem. This generalizes one of the main results of Anderson-Griffeth-Miller (which was conjectured earlier by Graham-Kumar) from the finite to any symmetrizable Kac-Moody case. **THEOREM.** For any  $u, v, w \in W$ ,

$$(-1)^{\ell(u)+\ell(v)+\ell(w)} p_{u,v}^w \in F_+[(e^{-\alpha_1} - 1), \dots, (e^{-\alpha_r} - 1)],$$

where  $\{\alpha_1, \dots, \alpha_r\}$  are the simple roots. (Received August 06, 2012)