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We introduce a notion of convex drawings of complete graphs, naturally leading to a hierarchy of drawings, from restrictive to general: rectilinear, face-convex, hereditarily-convex, convex and general topological. We present general results that shed light on Aichholzer's computer proof (personal communication) showing that all optimal drawings of  $K_n$  with  $n \leq 12$  are also convex drawings. We have distinguishing examples, characterizing theorems and many new and exciting open questions. (Received September 09, 2017)