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Monsikarn Jansrang* (jansr1m@cmich.edu). *Graph Complement Conjecture for Minimum Semidefinite Rank*. Preliminary report.

Given an $n \times n$ Hermitian matrix $A = [a_{ij}]$ we associate a graph $G(A)$ to the matrix A in such a way that the set of vertices is $\{v_1, \dots, v_n\}$ and the set of edges is $E = \{\{v_i, v_j\} : a_{ij} \neq 0, i \neq j\}$. The diagonal entries of A do not have an effect on $G(A)$. Let $P(G) = \{A \in M_n(\mathbb{C}) : A^* = A, A \text{ is positive semidefinite, } G(A) = G\}$. The *minimum semidefinite rank* of G is defined to be $mr_+^{\mathbb{C}}(G) = \min\{\text{rank}(A) : A \in P(G)\}$. If we restrict to real symmetric positive semidefinite matrices the real minimum semidefinite rank is denoted by $mr_+^{\mathbb{R}}(G)$ and it is clear that $mr_+^{\mathbb{C}}(G) \leq mr_+^{\mathbb{R}}(G)$.

It has been conjectured that $mr_+^{\mathbb{R}}(G) + mr_+^{\mathbb{R}}(\overline{G}) \leq |G| + 2$ where \overline{G} is the complement of the graph G and $|G|$ is the number of vertices in G . This conjecture is called “Graph Complement Conjecture” and is denoted GCC_+ . In this talk we will mention some known results on GCC_+ and some new results about certain bipartite graphs. (Received September 24, 2017)