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77553. *On Metric Dimension of Permutation Graphs*. Preliminary report.

The *metric dimension*  $\dim(G)$  of a graph  $G$  is the minimum number of vertices such that every vertex of  $G$  is uniquely determined by its vector of distances to the set of chosen vertices. Let  $G_1$  and  $G_2$  be disjoint copies of a graph  $G$ , and let  $\sigma : V(G_1) \rightarrow V(G_2)$  be a permutation. Then, a *permutation graph*  $G_\sigma = (V, E)$ , in the sense of Chartrand and Harary, has the vertex set  $V = V(G_1) \cup V(G_2)$  and the edge set  $E = E(G_1) \cup E(G_2) \cup \{uv \mid v = \sigma(u)\}$ . We show that  $2 \leq \dim(G_\sigma) \leq n - 1$  for any connected graph  $G$  of order  $n \geq 3$ . We give examples showing that neither is there a function  $f$  such that  $\dim(G) < f(\dim(G_\sigma))$  for all pairs  $(G, \sigma)$ , nor is there a function  $g$  such that  $g(\dim(G)) > \dim(G_\sigma)$  for all pairs  $(G, \sigma)$ . Further, we characterize permutation graphs  $G_\sigma$  satisfying  $\dim(G_\sigma) = n - 1$  when  $G$  is a complete  $k$ -partite graph, a cycle, or a path on  $n$  vertices. (Received June 28, 2012)