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**Cassie L Williams\*** ([willi5cl@jmu.edu](mailto:willi5cl@jmu.edu)), James Madison University, Harrisonburg, VA. *Lattices of orders, conjugacy classes of matrices, and isogeny of abelian varieties*. Preliminary report.

An isogeny class of abelian varieties over  $\mathbb{F}_p$  is determined by the characteristic polynomial of its Frobenius endomorphism,  $f$ . For elliptic curves, one can find a formula for the size of such an isogeny class by summing class numbers of members of a certain lattice of orders in a quadratic imaginary field. In 2003, Gekeler related a proportion of matrices with characteristic polynomial  $f$  to these class numbers, and thus to the size of a chosen isogeny class. To extend, we compute the analogous ratio of matrices in  $\mathrm{GSp}_4$  and find a relation to a ratio of class numbers in a quartic imaginary field. Then we use an appropriate lattice of orders and results of Everett Howe to work towards a formula for the size of an isogeny class of abelian surfaces. (Received September 10, 2013)