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92093. *Bounds for B_k^+ -sets.*

A set $A \subset \mathbb{Z}$ is a B_k^+ -set if

$$a_1 + \cdots + a_k = b_1 + \cdots + b_k \text{ with } a_1, \dots, a_k, b_1, \dots, b_k \in A \tag{1}$$

implies $a_i = b_j$ for some $1 \leq i, j \leq k$. A is a B_k -set if (1) implies (a_1, \dots, a_k) is a permutation of (b_1, \dots, b_k) . The problem of determining the largest B_k -set $A \subset [N]$ has been studied extensively. In this talk we will discuss the corresponding problem for B_k^+ -sets. For odd $k \geq 3$, we use a Bose-Chowla B_k -set to construct a B_k^+ -set $A \subset [N]$ with $|A| = 2^{1-1/k}N^{1/k} - o(N^{1/k})$. We use a combinatorial argument to prove non-trivial upper bounds on B_3^+ -sets and B_4^+ -sets. (Received August 23, 2012)