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Lucas Kramer and **Ryan R. Martin*** (rymartin@iastate.edu), 396 Carver Hall, Department of Mathematics, Iowa State University, Ames, IA 50011, and **Michael Young**. *Diamond-free families in the Boolean lattice.*

For a family of subsets of $\{1, \dots, n\}$, ordered by inclusion, and a partially-ordered set P , we say that the family is P -free if it does not contain a subposet isomorphic to P . We want to compute $\text{ex}(n, P)$, the largest size of a P -free family of subsets of $\{1, \dots, n\}$. It is conjectured that, for any fixed P , this quantity is $(k + o(1))\binom{n}{\lfloor n/2 \rfloor}$ for some fixed integer k , depending only on P . The conjecture has been verified by Bukh in the case where P has a “tree shape”. There are some other small posets P for which the conjecture has been verified. The smallest poset for which it is unknown is Q_2 , the Boolean lattice on two elements. We will discuss improved bounds on the size of a Q_2 -free family, utilizing Razborov’s flag algebra method. (Received August 09, 2012)