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**Michael Bukatin\*** (bukatin@cs.brandeis.edu), **Ralph Kopperman** (rdkcc@ccny.cuny.edu) and **Steve Matthews** (steve.matthews@warwick.ac.uk). *Enrichment in Quantaloids: a Typed Enrichment for Categorical Description of Heterogenous Spaces.*

Typed enrichment is a situation where an arrow between objects  $X$  and  $Y$  is selected from a category determined by  $(Type(X), Type(Y))$ .

The enrichment in quantaloids is a version of enrichment in bicategories greatly simplified conceptually and technically by the restrictive requirement that the categories corresponding to  $(Type(X), Type(Y))$  be complete lattices.

There has been a lot of interest in quantaloid enrichment in recent years. In particular, it was used to produce categorification of spaces of partially defined elements, such as lattice-valued sets and partial metric spaces.

This categorification sheds additional light on the meaning of the strong triangularity axiom of partial metrics,  $P(X, Z) \leq P(X, Y) + P(Y, Z) - P(Y, Y)$ . The typed composition,  $P(X, Y) \circ_Y P(Y, Z) = P(X, Y) + P(Y, Z) - P(Y, Y)$ , is defined in such a fashion that self-distances of partially defined points,  $P(Y, Y)$ , are units with respect to the composition  $P(X, Y) \circ_Y P(Y, Z)$ , despite those self-distances generally being non-zero. (Received September 03, 2012)