

1084-13-127

**Bruce Olberding\*** (olberdin@nmsu.edu), Department of Mathematical Sciences, New Mexico State University, Las Cruces, NM 88003-8001, and **Francesca Tartarone** (tfrance@mat.uniroma3.it), Dipartimento di Matematica, Università degli Studi “Roma Tre”, Largo San Leonardo Murialdo 1, 00146 Roma, Italy. *Integrally closed rings in birational extensions of two-dimensional regular local rings.*

Let  $D$  be an integrally closed local Noetherian domain of Krull dimension 2, and let  $f$  be a nonzero element of  $D$ . Motivated by the problem of classifying the integrally closed rings  $H$  between  $D$  and  $D[1/f]$ , we consider when  $H$  is determined locally by finitely many valuation overrings of  $D$ , in the sense that if  $M$  is a maximal ideal of  $H$ , then there are finitely many valuation overrings  $V_1, \dots, V_n$  of  $D$  such that  $H_M = V_1 \cap \dots \cap V_n \cap (D_f)_M$ . (With such a representation, it is possible to describe the structure of the ring  $H_M$  in some detail.) In some central cases where  $D$  is a regular local ring and  $f$  is a regular parameter of  $D$ , then  $H$  is determined locally by a single valuation. As a “Noetherian” consequence, we show that with such a choice of  $D$  and  $f$ , if  $H$  is normalization of a finitely generated  $D$ -subalgebra of  $D_f$ , then the height one prime ideals of  $H$  lying over the maximal ideal of  $D$  are comaximal. Geometrically, this translates into a statement about intersections of irreducible components in the closed fiber of the normalization of a proper birational morphism. (Received August 28, 2012)