

1084-16-139

**Louis H. Rowen\*** (rowen@math.biu.ac.il), 52900 Ramat-Gan, Israel. *Representability of algebras finite over their centers.*

(Joint work with L. Small)

An algebra  $R$  (not necessarily associative) over a central subring  $Z$ , is called **representable** if, for a suitable field  $K$ ,  $R$  is embeddable as a  $C$ -subalgebra of a finite dimensional  $K$ -algebra  $W$ .  $R$  is **strongly representable** if  $W$  can be taken to be the localization  $S^{-1}R$  for some multiplicative submonoid  $S$  of  $Z$ .

The motivation comes from the associative theory, in which case we could take  $W = M_n(K)$  for suitable  $n$ .

Beidar [?] proved that any associative algebra finite (as a module) over a commutative Noetherian affine algebra over a field is representable, and his theorem turns out to be required for other important theorems in PI-theory. Anan'in proved more generally that every left Noetherian PI-algebra that is affine over a field is representable.

An algebra is called **weakly Noetherian** if it satisfies the ACC on ideals. We prove (with a straightforward argument):

**Theorem A:** If a weakly Noetherian algebra  $R$  is finite (as a module) over a central subalgebra  $Z$  which contains a field  $F_0$ , then  $R$  is a finite subdirect product of strongly representable algebras.

Theorem A fails when we weaken its hypotheses. Other related results are also presented. (Received August 29, 2012)