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**Sergejs Solovjovs\*** (solovjovs@math.muni.cz), Department of Mathematics and Statistics,  
Faculty of Science, Masaryk University, Kotlarska 2, 611 37 Brno, Czech Rep. *Tower extension of  
topological categories.*

Given a topological construct  $\mathbf{C}$  and a completely distributive lattice  $L$ , D. Zhang presented in 2000 a procedure of obtaining a new topological construct  $\mathbf{C}(L)$ , called the *tower extension of  $\mathbf{C}$  w.r.t.  $L$* , which provided a common setting for various existing topological machineries (e.g., the construction of the category of *approach spaces* of R. Lowen). Being implicitly a kind of a fuzzification of topological constructs, tower extension of D. Zhang fails to be well related to fuzzy topology. To remove the deficiency, we present its “partial” dualization called *tower extension of topological categories*, which, firstly, is applicable to (almost) every topological category; secondly, is variable-basis, namely, can rely on a whole category of lattice-theoretic structures in the sense of S. E. Rodabaugh; and, thirdly, for suitable categories  $\mathbf{C}$ , it produces the categories of fuzzy topological spaces in the sense of U. Höhle, T. Kubiak and A. Šostak. As a consequence, we conclude that the fuzzification framework of U. Höhle, T. Kubiak, A. Šostak and the approach framework of R. Lowen are “partially” dual to each other.

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