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I. M. Isaacs* (isaacs@math.wisc.edu), **Maria Loukaki** and **Alexander Moreto**. *The average degree of an irreducible character.*

Let G be a finite group, and write $\text{acd}(G) = \sum \chi(1)/|\text{Irr}(G)|$, where the sum runs over $\chi \in \text{Irr}(G)$. Then $\text{acd}(G)$ is the average of the degrees of the irreducible characters of G , and it is easy to see that $\text{acd}(G) = 1$ if and only if G is abelian. This suggests that if $\text{acd}(G)$ is small, then G should be “almost” abelian. We show that if $\text{acd}(G) \leq 3$, then G is solvable. (Since $\text{acd}(A_5) = 3.2$, our result is probably not best-possible.) We also show that G is supersolvable if $\text{acd}(G) \leq 3/2$ and G is nilpotent if $\text{acd}(G) \leq 4/3$. (Received August 14, 2012)