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Roger Nichols* (roger-nichols@utc.edu). *Positivity Preserving of Semigroups and Resolvents of Sturm–Liouville-type Operators with Distributional Coefficients*. Preliminary report.

In this talk, we consider self-adjoint extensions of the minimal operator associated with Sturm–Liouville-type differential expressions,

$$\tau f = \frac{1}{r} \left(- (p[f' + sf])' + sp[f' + sf] + qf \right) \text{ on } (a, b) \subset \mathbb{R},$$

where the coefficients p, q, r, s are real-valued and Lebesgue measurable on (a, b) , with $p \neq 0, r > 0$ a.e. on (a, b) , and $p^{-1}, q, r, s \in L^1_{\text{loc}}((a, b); dx)$, and f belongs to a suitably wide class of functions. In the case where τ is regular on (a, b) (i.e., when (a, b) is a finite interval and $L^1_{\text{loc}}((a, b); dx)$ above may be replaced by $L^1((a, b); dx)$), all self-adjoint extensions of the minimal operator are characterized by boundary conditions at a and b . Using integral operator techniques and the Beurling–Deny criterion, under the assumption $p > 0$ a.e. on (a, b) , we classify all boundary conditions leading to self-adjoint extensions which generate a positivity preserving semigroup (equivalently, resolvent).

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