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Arunima Ray* (arunima.ray@rice.edu). *Slice knots which bound Klein bottles.*

We investigate the properties of knots in \mathbb{S}^3 which bound Klein bottles, such that a pushoff of the knot has zero linking number with the knot, i.e. has *zero framing*. This is motivated by the many results in the literature regarding slice knots of genus one, for example, the existence of homologically essential zero self-linking simple closed curves on genus one Seifert surfaces for algebraically slice knots. Given a knot K bounding a (punctured) Klein bottle F with zero framing, we show that J , the core of the orientation-preserving band in any disk-band form of F , has zero self-linking. We prove that such a K is slice in a $\mathbb{Z}[\frac{1}{2}]$ -homology \mathbb{B}^4 if and only if J is as well, a stronger result than what is currently known for genus one slice knots. As an application, we prove that given knots K and J and any odd integer p , the $(2, p)$ cables of K and J are $\mathbb{Z}[\frac{1}{2}]$ -concordant if and only if K and J are $\mathbb{Z}[\frac{1}{2}]$ -concordant. In particular, if the $(2, 1)$ -cable of a knot K is slice, K is slice in a $\mathbb{Z}[\frac{1}{2}]$ -homology ball. (Received August 23, 2012)