

1084-68-132

Feodor F. Dragan* (dragan@cs.kent.edu), Department of Computer Science, Kent State University, Kent, OH 44242, and **Muad Abu-Ata**. *Collective Additive Tree Spanners of Bounded Tree-Breadth Graphs with Generalizations and Consequences*.

We study collective additive tree spanners for families of graphs enjoying special Robertson-Seymour's tree-decompositions, and demonstrate interesting consequences of obtained results. It is known that if a graph G has a multiplicative tree t -spanner, then G admits a Robertson-Seymour's tree-decomposition with bags of radius at most $\lceil t/2 \rceil$ in G . We use this to demonstrate that there is a polynomial time algorithm that, given an n -vertex graph G admitting a multiplicative tree t -spanner, constructs a system of at most $\log_2 n$ collective additive tree $O(t \log n)$ -spanners of G . That is, with a slight increase in the number of trees and in the stretch, one can "turn" a multiplicative tree spanner into a small set of collective additive tree spanners. We extend this result by showing that, for every fixed k , there is a polynomial time algorithm that, given an n -vertex graph G admitting a multiplicative t -spanner with tree-width $k - 1$, constructs a system of at most $k(1 + \log_2 n)$ collective additive tree $O(t \log n)$ -spanners of G . (Received August 28, 2012)