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**Amanda Croll\***, 203 Avery Hall, University of Nebraska-Lincoln, P.O. Box 880130, Lincoln, NE 68505. *Periodic modules over a Gorenstein local ring*. Preliminary report.

This work concerns finitely generated modules over a commutative Gorenstein local ring  $R$ . It is proved that the minimal free resolution of such a module  $M$  is eventually periodic if, and only if, the class of  $M$  is torsion in a certain  $\mathbb{Z}[t, t^{-1}]$ -module associated to  $R$ . This module, which we denote  $J_R(t)$ , is a quotient of the free  $\mathbb{Z}[t, t^{-1}]$ -module on the isomorphism classes of finitely generated  $R$ -modules by relations reminiscent of those defining the Grothendieck group of  $R$ . The main result is a structure theorem for  $J_R(t)$  when  $R$  is a complete Gorenstein local ring; the link between periodicity and torsion stated above is a corollary. As a consequence, a complete Gorenstein local ring has an eventually periodic module if and only if the module  $J_R(t)$  has nontrivial torsion. (Received September 09, 2012)