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Sean Sather-Wagstaff* (sean.sather-wagstaff@ndsu.edu). *Weakly Spherical DG Modules over Koszul Complexes*. Preliminary report.

Let (R, \mathfrak{m}, k) be a commutative local noetherian ring, and let $K = K^R(\mathbf{x})$ be the Koszul complex over R on the sequence $\mathbf{x} = x_1, \dots, x_n \in \mathfrak{m}$. Given an integer $n \geq 1$, a homologically finite DG K -module X is *weakly n -spherical* if

$$\mathrm{Ext}_R^i(X, X) \cong \begin{cases} 0 & \text{for } i \neq 0, n \\ k & \text{for } i = 0, n. \end{cases}$$

(This definition is motivated by the notion of “spherical objects” from derived algebraic geometry.) For instance, if R is a DVR, then k is a weakly 1-spherical DG R -module. We prove (a) this is essentially the only way to construct weakly n -spherical DG R -modules, and (b) for $n \neq 2$, this is essentially the only way to construct weakly n -spherical DG K -modules. (Received August 26, 2012)