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**Jorge M Ramirez\*** (jmramirezo@unal.edu.co), Calle 59A No 63-20, Bloque 43 - 242, Medellin, Antioquia 05001000, Colombia. *Diffusion processes on graphs: construction and applications.*

Consider a graph  $\Gamma$  consisting of infinite edges  $e_0, e_1, e_2$  joined at node  $\phi$ . A function  $f : \Gamma \rightarrow \mathbb{R}$  is specified by its restrictions  $f_i : [0, \infty) \rightarrow \mathbb{R}$  to each of the edges. For positive, non-zero numbers  $D_i$ ,  $i = 0, 1, 2$ , we consider parabolic operators acting on functions over  $\Gamma$ . One example is the operator  $A$  given by  $(Af)_i = D_i f_i''$  acting on functions that are smooth inside each edge of  $\Gamma$ , and satisfy the flux condition  $\sum_i D_i f_i'(0^+) = 0$ , at node  $\phi$ . The associated stochastic process  $\{X(t) : t \geq 0\}$  is a Feller process on  $\Gamma$  that has  $A$  as its infinitesimal generator. The sample paths of  $X$  behave like (appropriately re-scaled) Brownian motion inside each edge, but have different transition probabilities from the node into each of the adjoining edges, generalizing the notion of “skew Brownian motion” to a graph. Application examples include dispersion phenomena in river systems, blood vessels, and electrical networks. In this talk we also consider, in particular, the case where the diffusion process contains a non-zero advection term, e.g.  $(Af)_i = D_i f_i'' + v_i f'$ . (Received August 14, 2012)