

1094-60-342

**Mauro Maggioni\*** (mauro@math.duke.edu), BOX 90320, Department of Mathematics, Duke University, Durham, NC 27708. *Geometric Multi-Resolution Analysis and Approximation of probability measures in high dimensions.*

Given  $n$  i.i.d. samples from a probability measure  $\mu$  in  $\mathbb{R}^D$ , we study the problem of constructing efficiently an approximation  $\hat{\mu}_n$  that is close to  $\mu$  in a Wasserstein metric. The approximation scheme we propose is suited for the situation when  $\mu$  is concentrated near a locally-linear low-dimensional set. This is motivated by the analysis of large data sets in high-dimensions, which in many applications appear to have low intrinsic dimension. Our construction is based on a hierarchical multi-resolution analysis on the data, where at each level of a hierarchy an approximation to  $\mu$  is constructed, and is suitably refined at finer scales depending on the number of samples available and on the complexity of  $\mu$ . The approximation guarantees are, under suitable assumptions on  $\mu$ , independent of the ambient dimension, are non-asymptotic, and show that with high probability we obtain an estimator  $\hat{\mu}_n$  of  $\mu$  that approximates  $\mu$  suitably rapidly in  $n$ . Fast algorithms implement this construction and applications will be demonstrated to real world data sets. (Received August 27, 2013)