

1111-13-41

**Shalom Eliahou\*** ([eliahou@lmpa.univ-littoral.fr](mailto:eliahou@lmpa.univ-littoral.fr)), LMPA-ULCO, 50, rue Ferdinand Buisson, CS 80699, 62228 Calais, France. *Some progress towards Wilf's conjecture.*

Let  $S$  be a numerical semigroup, i.e. a subset of  $\mathbb{N}$  containing 0, closed under addition and with finite complement in  $\mathbb{N}$ . This last condition means that a suitable translate  $c + \mathbb{N} = \{c, c + 1, c + 2, \dots\}$  of  $\mathbb{N}$  is contained in  $S$ . The smallest such integer  $c$  is known as the conductor of  $S$ . Let  $e$  be the embedding dimension of  $S$ , i.e. its least number of generators. Let also  $m$  be the multiplicity of  $S$ , i.e. its smallest non-zero element. In 1978, Wilf conjectured that the number of elements in  $S$  which are smaller than  $c$  is bounded below by  $c/e$ . Wilf's conjecture is known to hold in various cases, including when  $c \leq 2m$ . In this talk, we settle Wilf's conjecture in the case where  $c \leq 3m$ , which asymptotically represents, in an appropriate sense, the majority of numerical semigroups. One main ingredient in our proof is a classical theorem of Macaulay on the growth of Hilbert functions of standard graded algebras. (Received January 09, 2015)