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**Vigneron-Tenorio** (alberto.vigneron@uca.es), Dpto. Matemáticas, Facultad de Ciencias Sociales, y de la Comunicació, 11405 Jerez de la Fra., Cádiz, Spain. *Affine convex body semigroups of  $\mathbb{N}^3$* . Preliminary report.

Let  $F$  be a subset of  $\mathbb{R}^k$  with non-empty interior,  $\mathcal{F} = \cup_{i=0}^{\infty} F_i \cap \mathbb{N}^k$ , where  $F_i = \{iX \mid X \in F\}$  with  $i \in \mathbb{N}$ . A convex body of  $\mathbb{R}^n$  is a compact convex subset of  $\mathbb{R}^n$  with non-empty interior. If  $F$  is a convex body, then the set  $\mathcal{F}$  is a semigroup of  $\mathbb{N}^k$ , the convex body semigroup generated by  $F$ . This kind of semigroups generalize to arbitrary dimension the concept of proportionally modular numerical semigroup.

In general, these semigroups are not finitely generated. If  $\mathcal{F}$  is a finitely generated semigroup we say that  $\mathcal{F}$  is an affine convex body semigroup. In previous works, convex body semigroups generated by polygons of  $\mathbb{N}^2$  have been studied. We have characterizations to check if a convex body semigroup is finitely generated. It must be noted that these semigroups provides us with instances of families of Cohen-Macaulay semigroups and examples of Gorenstein semigroups.

In our work we study convex body semigroups when  $F$  is a convex polyhedron of  $\mathbb{R}^3$ , characterizing affine convex body semigroups of  $\mathbb{N}^3$  and giving some results concerning the Cohen-Macaulay property. (Received February 10, 2015)