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The concept of non-separating cocircuit in a binary matroid is the closer concept for matroids to the one of vertices in graphs. A cocircuit C^* in a connected matroid M is said to be *non-separating* if $M \setminus C^*$ is a connected matroid. For a 3-connected graph G , the unique non-separating cocircuits of $M(G)$ are the stars of the vertices of G .

Let M be a 3-connected binary matroid with more than four elements. Bixby and Cunningham proved that M is graphic if and only if, in M , each element belongs to at most two non-separating cocircuits. Lemos proved that M is graphic if and only if each elements of M avoids at most $r^*(M) - 1$ non-separating cocircuits. In this work we study the set $Y(M)$ of the elements of M avoiding at least $r^*(M)$ non-separating cocircuits of M . We proved that if M is not graphic, $|E(M) - Y(M)| \leq 1$ when M is not regular or M has no $K'''_{3,3}$ -minor. We have a conjecture that if M is not graphic, then $r^*_M(E(M) - Y(M)) \leq 2$. We proved that this conjecture is valid in general if and only if it holds on a determined finite class of matroids. The computational procedure to finish the proof of the conjecture is in course. (Received November 15, 2012)