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Thai Hoang Le* (leth@math.utexas.edu) and **Craig Spencer**. *Intersective polynomials and Diophantine approximation.*

It has been known since Vinogradov that for each k , there is an exponent $\theta = \theta(k)$ such that for every positive integer N and real number α , we have $\min_{1 \leq n \leq N} \|\alpha n^k\| \ll N^{-\theta}$, the bound being uniform in α and N (where $\|\cdot\|$ denotes the distance to the nearest integer). More generally, there is an exponent $\theta = \theta(k, l)$ such that for any polynomials f_1, \dots, f_l of degree at most k and with zero constant terms, we have $\min_{1 \leq n \leq N} \|\max_{1 \leq i \leq l} f_i(n)\| \ll N^{-\theta}$, the bound being uniform in the coefficients of f_1, \dots, f_l . Much effort has been put in finding best possible exponents. In joint work with Craig Spencer, we generalize further the above results, replacing each monomial n^k by a polynomial in $\mathbf{Z}[x]$. It turns out that the only obstructions to the above inequalities are of local nature. (Received November 27, 2012)