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**Pieter C Allaart\*** (allaart@unt.edu), Mathematics Department, 1155 Union Circle #311430, Denton, TX 76203-5017. *The Hausdorff dimension of level sets of generalized Takagi functions*. Preliminary report.

Takagi's continuous but nowhere differentiable function is defined by

$$T(x) = \sum_{n=0}^{\infty} \frac{1}{2^n} \phi(2^n x),$$

where  $\phi(x)$  is the distance from  $x$  to the nearest integer. Recently there has been a great deal of interest in the level sets of  $T$ , which have been shown to possess many surprising properties. In particular it is now known that the maximal Hausdorff (and box-counting) dimension of the level sets of  $T$  is  $1/2$ . This talk concerns the dimension of level sets of the more general functions of the form

$$f(x) = \sum_{n=0}^{\infty} \frac{\omega_n(x)}{2^n} \phi(2^n x),$$

where each  $\omega_n$  is a  $\{-1, 1\}$ -valued function which may jump only at points  $k/2^n$ , so that each term of the above series is a continuous function. For such functions, the dimension of the level sets can be considerably greater than  $1/2$ . A sharp upper bound for this dimension will be presented, but on the other hand, it will be shown that the original bound of  $1/2$  remains valid in the special case when each  $\omega_n$  is constant. If time permits, the case when the sign functions  $\omega_n$  are chosen at random will also be discussed. (Received November 27, 2012)