Under the strong open set condition we have determined the bounds of the lower and the upper quantization dimensions of a probability measure supported by the limit set of a recurrent hyperbolic iterated function system. Moreover, we have shown that the lower and upper bounds are related with the temperature functions of the thermodynamic formalism corresponding to the lower and upper contractive ratios of the hyperbolic maps. (Received December 02, 2012)