

1087-42-55

**Oleksandr (Alexander) V Tovstolis\*** (atovstolis@math.okstate.edu), Department of Mathematics, Oklahoma State University, 401 Mathematical Sciences, Stillwater, OK 74078.  
*Fourier Multipliers in Hardy Spaces and Some Inequalities of Approximation Theory.*

Let  $\mathcal{M}_{p,q}(T_\Gamma)$  denotes the class of Fourier multipliers from  $H^p(T_\Gamma)$  to  $H^q(T_\Gamma)$ ,  $0 < p \leq q \leq 1$ , in tubes over a regular cone  $\Gamma \subset \mathbb{R}^n$  (i.e., the dual cone,  $\Gamma^*$ , has non-empty interior).

Several conditions for multipliers are obtained. They could be successfully applied to problems of Approximation Theory. For example, the critical index for Bochner-Riesz means was found.

If a function belonging to  $H^p$  is also an entire function of exponential type, then the following Bernstein-type inequality holds true.

**Theorem 1** *Let  $p \in (0, \infty)$ , and  $K$  be a symmetric body in  $\mathbb{R}^n$ . Then, for  $f \in \mathcal{E}(K^*) \cap H^p(T_\Gamma)$  and a multi-index  $k = (k_1, \dots, k_n)$ ,*

$$\left\| \frac{\partial^{|k|} f}{\partial z_1^{k_1} \dots \partial z_n^{k_n}} \right\|_{H^p} \leq (2\pi)^{|k|} \prod_{j=1}^n \sigma_j^{k_j} \|f\|_{H^p},$$

where  $\sigma_j := \max_{t \in K \cap \Gamma^*} |t_j|$ ,  $|k| = k_1 + \dots + k_n$ .

Some Nikolskii's type inequalities are also obtained. (Received November 24, 2012)