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The Ripley k -function is used to study the distribution of random points in a planar area or in three space. If the points are distributed by a Poisson process, then they tend to cluster around a line. The formal function is given by

$$K_n(h) = \sqrt[n]{\sum_{i=1}^m \sum_{j \neq i} \frac{I_h(i, j)}{m \cdot (m - 1)}}$$

The function $I_h(i, j)$ is 1 if $d(x_i, x_j) < h$ and is 0 if $d(x_i, x_j) \geq h$ where the random points are $\{x_i\}_{i=1}^m$. The n in the formula is given by $n = 2$ if the points are in a planar area or $n = 3$ if in a three-dimensional area.

Suppose that the points are distributed randomly based on Hausdorff measure on a self-similar fractal. Would some analysis similar to the Ripley k -function apply in this case? We can show that such a random set of points can be used to give a reliable estimate of the Hausdorff dimension of the self-similar fractal. We will explain the theory and demonstrate its implementation. We will also discuss applications of the theory. (Received December 03, 2012)