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**Florian Enescu** (fenescu@gsu.edu) and **Yongwei Yao\*** (yyao@gsu.edu), Department of Math & Stat, Georgia State University, Atlanta, GA 30303. *The Frobenius Complexity*. Preliminary report.

Let  $R$  be a commutative ring with prime characteristic  $p$ . For any  $R$ -module  $M$ , there is *algebra of Frobenius operators*

$$\mathcal{F}(M) := \bigoplus_{e \geq 0} \mathcal{F}^e(M)$$

in which  $\mathcal{F}^e(M)$  consists of all  $\mathbb{Z}$ -linear maps  $h: M \rightarrow M$  such that  $h(rm) = r^{p^e}h(m)$  for all  $r \in R$  and  $m \in M$ . A very interesting case is when  $M = E := E_R(R/\mathfrak{m})$  over a local ring  $(R, \mathfrak{m})$ ; and there are several ways to interpret the ring  $\mathcal{F}(E)$ .

As  $\mathcal{F}(E)$  may not be finitely generated over  $\mathcal{F}^0(E)$  in general, we would like to find ways to measure how far away  $\mathcal{F}(E)$  is from being finitely generated over  $\mathcal{F}^0(E)$ . In particular, we define the *Frobenius complexity* of  $\mathcal{F}(E)$ .

Moreover, cases of low dimension are examined. Some concrete examples are computed. This is joint work with Florian Enescu. (Received August 13, 2013)