Tolga Karayayla* (tkarayay@metu.edu.tr), Department of Mathematics, Middle East
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Groups of Rational Elliptic Surfaces with Section and Constant J-Map.

I will present the second leg of the classification project for the automorphism groups of rational elliptic surfaces (RES) with section which concerns those RES with constant J-Map. In the first leg of this study, it was shown that the group Aut(B) of regular automorphisms (biholomorphic maps) of a relatively minimal RES B over the field \mathbb{C} is the semi-direct product $MW(B) \times Aut_{\sigma}(B)$ of its Mordell-Weil group MW(B) (the group of sections) and the subgroup $Aut_{\sigma}(B)$ of the automorphisms preserving the zero section of the surface. MW(B) has been classified by Oguiso and Shioda with respect to the configuration of singular fibers on B. $Aut_{\sigma}(B)$ was classified for RES with non-constant J-Map in the first leg of this study. In this talk I will discuss the results in the constant J-Map case. RES with constant J-Map have richer automorphism groups. While $Aut_{\sigma}(B)$ has size at most 24 in the non-constant J-Map case, it can have size 144 or can even be infinite depending on the configuration of singular fibers on B if the J-Map is constant. One reason for having more symmetry in that second case is the existence of automorphisms which act as complex multiplication of order 3,4 or 6 on every smooth elliptic curve fiber of the surface. (Received June 17, 2013)