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Kathryn Mann* (mann@math.uchicago.edu). *Components of representation spaces.*

Let G be a group of homeomorphisms of the circle, and Γ the fundamental group of a closed surface. The representation space $\text{Hom}(\Gamma, G)$ is a basic example in geometry and topology: it parametrizes flat circle bundles over the surface with structure group G , or G -actions of the surface group on the circle. Goldman proved that connected components of $\text{Hom}(\Gamma, \text{PSL}(2, \mathbb{R}))$ are completely determined by the Euler number, a classical invariant. By contrast, the space $\text{Hom}(\Gamma, \text{Homeo}^+(S^1))$ is relatively unexplored – for instance, it is an open question whether this space has finitely or infinitely many components.

We report on recent work and new tools to distinguish connected components of $\text{Hom}(\Gamma, \text{Homeo}^+(S^1))$. In particular, we give a new lower bound on the number of components, show that there are multiple components on which the Euler number takes the same value – in contrast to the $\text{PSL}(2, \mathbb{R})$ case – and we identify certain representations which exhibit surprising rigidity. A key technique is the study of rigidity phenomena in rotation numbers, using recent ideas of Calegari-Walker. (Received August 15, 2013)