

1100-30-102

Tom D Downs* (proftddowns@msn.com), 12411 Calico Falls Lane, Houston, TX 77041. *Complex Functions and Spherical Regression.*

Polar forms below provide insight and clarity into potential uses of the bilinear functions M_c for dealing with otherwise difficult or insurmountable problems. Let S be a Riemann sphere centered at the origin 0 of a Euclidean space with an xyt rectangular coordinate system and horizontal extended complex equatorial plane C . The vertical polar axis of S is the t -axis, which intersects S at the poles $n=(001)$ and $s=(00-1)$, and C at 0 . This is a rigid configuration. Stereographic projections map unit vectors $Z=(xyt)$ on S to points $z=x+iy$ on C , and vice versa, when the 3 points n,Z,z are collinear. The points n on S and ∞ on C are designated images of one another. Bilinear functions M_c map C on to itself and form a group G_1 under composition of mappings; their matrix images also form a group under matrix multiplication. The spherical images M of the M_c operate on points Z on S to form a group G_2 under composition of mappings. G_2 is isomorphic to G_1 . For any M_c in G_1 the identity $M_c \equiv \{M_c/\sqrt{(M_c^*M_c)}\}x\{\sqrt{(M_c^*M_c)}\} = \{U_c\}x\{H_c\}$ holds, where $*$ means the conjugate transpose of M_c , U_c is unitary, and H_c is pos. def. hermitian with decomposition $H_c = B^*\Delta B$ where B is unitary and Δ is diagonal. Analogous decompositions apply to the images M of G_2 . (Received February 03, 2014)