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**Murat Akman\*** ([murat.akman@uky.edu](mailto:murat.akman@uky.edu)), Department of Mathematics, University of Kentucky, Lexington, KY 40508. *On the Hausdorff dimension of a measure arising from a positive weak solution to a quasilinear elliptic PDE in the plane.* Preliminary report.

In this talk we study the Hausdorff dimension of a measure  $\mu_f$  related to a positive weak solution,  $u$ , of a certain quasilinear elliptic partial differential equation in  $\Omega \cap N$  where  $\Omega \subset \mathbb{C}$  is a bounded simply connected domain and  $N$  is a neighborhood of  $\partial\Omega$ .  $u$  has continuous boundary value 0 on  $\partial\Omega$  and is a positive weak solution to

$$\sum_{i,j=1}^2 \frac{\partial}{\partial x_i} (f_{\eta_i \eta_j}(\nabla u(z)) u_{x_j}(z)) = 0 \text{ in } \Omega \cap N.$$

Also  $f(\eta)$ ,  $\eta \in \mathbb{R}^2$  is homogeneous of degree  $p$ ,  $1 < p < 2$ , and uniformly convex in the plane. Put  $u \equiv 0$  in  $N \setminus \Omega$ . Then  $\mu_f$  is the unique positive finite Borel measure, called generalized  $p$ -harmonic measure, with support on  $\partial\Omega$ .

Then it is shown that  $\mu_f \ll \mathcal{H}^\lambda$  for  $1 < p < 2$  where

$$\lambda(r) = r \exp A \sqrt{\log 1/r \log \log \log 1/r}, 0 < r < 10^6.$$

Our work generalizes work of Lewis in [L12] when the above PDE is the  $p$ -Laplacian,  $1 < p < 2$ , (i.e,  $f(\eta) = |\eta|^p$ ) in the complete generalization.

[L12]: John Lewis.  $p$ -harmonic measure in simply connected domains revisited. Transactions of the American Mathematical Society, To appear. (Received February 04, 2014)