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Mikhail D Surnachev* (peitsche@yandex.ru), Keldysh Institute of Applied Mathematics, Miusskaya Sq. 4, Moscow, 125047, Russia. *On regularity of solutions to nonlinear parabolic equations degenerating on a part of the domain.*

In this talk I will discuss regularity of solutions to nonlinear parabolic equations uniformly degenerating on a part of the domain. Consider the equation $\omega_\varepsilon(x)u_t = \operatorname{div}(\omega_\varepsilon(x)|\nabla u|^{p-2}\nabla u)$, $x = (x_1, \dots, x_n) \in \Omega \subset \mathbb{R}^n$, $t \in [0, T]$, where $\omega_\varepsilon(x_1, \dots, x_{n-1}, x_n) = 1$ if $x_n < 0$, $\omega_\varepsilon(x_1, \dots, x_{n-1}, x_n) = \varepsilon$ for $x_n > 0$. In any cylinder $(\Omega \cap \{|x_n| > \delta > 0\}) \times [0, T]$ the equation falls in the framework of the theory developed by E. DiBenedetto, U. Gianazza, V. Vespri and other authors - solutions are Hölder continuous, locally bounded, and satisfy an intrinsic form of Harnack's inequality. However, if we work in a domain which crosses the interface $\{x_n = 0\}$ the standard methods give results which degenerate with respect to the small parameter ε . I obtain regularity estimates independent of ε . This work extends earlier results obtained for the linear parabolic equations by Yu.A. Alkhutov and V. Liskevich. The method works for general nonlinear parabolic equations of the p-Laplace type. The author was partially supported by RFBR grant no. 12-01-00058-a and Russian Ministry of Science and Education grant no. 14.B37.21.0362 (Received February 08, 2014)