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Highly constrained edge-colorings of complete graphs, part II.

In this continuation of Part I, we discuss recent progress on several problems.

Let $\mathcal{C} = \{r, b_1, \dots, b_n\}$ and let $\mathcal{T} = \mathcal{C}^3 \setminus \{b_1, \dots, b_n\}^3$. Thus r is a *flexible color* in \mathcal{T} . Alm, Maddux, and Manske showed in 2007 that \mathcal{T} was realizable for all n using probabilistic methods. Recently, Alm and Sexton showed that for $n = 2$, \mathcal{T} is realizable on K_{8192} .

For \mathcal{T}_1 , it was known until recently only that \mathcal{T}_1 was realizable for $1 \leq n \leq 7$. The authors showed in 2013-14 that \mathcal{T}_1 is realizable for all $n \leq 400$, except possibly $n = 8$ and $n = 13$. Finally, the authors solved one of the two remaining minimal cases of the *flexible color conjecture*, where there are two colors, *red* and *directed blue*, and the only triangle that is forbidden is the “cycle” $\langle \overleftarrow{b}, \overrightarrow{b}, \overrightarrow{b} \rangle$.

All of these recent results were obtained using computational methods on finite groups. (Received July 28, 2014)