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**Dara Moazzami\*** ([dmoazzami@ut.ac.ir](mailto:dmoazzami@ut.ac.ir)), Prof. Mathematics, University of Tehran, College of Engineering, Department of Engineeg Science, Thehran, Iran. *On the Tenacity Parameter and Complexity of Recognizing Tenacious Graphs.*

The tenacity of a graph  $G$ ,  $T(G)$ , is defined by  $T(G) = \min\{\frac{|S| + \tau(G-S)}{\omega(G-S)}\}$ , where the minimum is taken over all vertex cutsets  $S$  of  $G$ . We define  $\tau(G-S)$  to be the number of the vertices in the largest component of the graph  $G-S$ , and  $\omega(G-S)$  be the number of components of  $G-S$ . A connected graph  $G$  is called  $T$ -tenacious if  $|S| + \tau(G-S) \geq T\omega(G-S)$  holds for any subset  $S$  of vertices of  $G$  with  $\omega(G-S) > 1$ . In this paper we consider the relationship between the minimum degree  $\delta(G)$  of a graph and the complexity of recognizing if a graph is  $T$ -tenacious. Let  $T \geq 1$  be a rational number. We first show that if  $\delta(G) \geq \frac{Tn}{T+1}$ , then  $G$  is  $T$ -tenacious. On the other hand, for any fixed  $\epsilon > 0$ , we show that it is  $NP$ -hard to determine if  $G$  is  $T$ -tenacious, even for the class of graphs with  $\delta(G) \geq (\frac{T}{T+1} - \epsilon)n$ .

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