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The twentieth century saw the elevation of Discrete Mathematics from "the slums of topology" to its current highly regarded position in the mathematical pantheon. Paul Erdős played a key role in this transformation. We will discuss some key results, possibly including:

- i) Ramsey Theory. In 1946 Erdős showed that you could two-color the complete graph on  $n$  vertices so as to avoid a monochromatic clique of size  $k$ , where  $n$  was exponential in  $k$ . To do it, he introduced The Probabilistic Method.
- ii) Random Graphs. The "phase transition" at  $e = v/2$  edges.
- iii) Crossing Number. We give a probabilistic argument to bound the crossing number of a graph on  $v$  vertices and  $e$  edges.
- iv) 2-Coloring. Given  $m$  sets, each of cardinality  $n$ , one wants to two-color the underlying points so that no set is monochromatic. In 1963 Erdős showed that this can be done if  $m < 2^{k-1}$  (color randomly!) and it remains an open question what is the largest  $m = m(n)$  for which such a coloring can always be found. We give a striking new argument of Kozik and Cherkashin, finding the best (so far!) lower bound on  $m(n)$ .

Anecdotes and personal recollections of Paul Erdős will be sprinkled liberally throughout the presentation. (Received July 14, 2014)