

1102-05-79

**Maria Axenovich\*** ([maria.aksenovich@kit.edu](mailto:maria.aksenovich@kit.edu)) and **Torsten Ueckerdt**. *Density of range capturing hypergraphs.*

For a finite set  $X$  of points in the plane, a set  $S$  in the plane, and a positive integer  $k$ , we say that a  $k$ -element subset  $Y$  of  $X$  is captured by  $S$  if there is a homothetic copy  $S'$  of  $S$  such that  $X \cap S' = Y$ , i.e.,  $S'$  contains exactly  $k$  elements from  $X$ . A  $k$ -uniform  $S$ -capturing hypergraph  $H = H(X, S, k)$  has a vertex set  $X$  and a hyperedge set consisting of all  $k$ -element subsets of  $X$  captured by  $S$ . In case when  $k = 2$  and  $S$  is convex these graphs are planar graphs, known as *convex distance function Delaunay graphs*.

We prove that for any  $k \geq 2$ , any  $X$ , and any convex compact set  $S$ , the number of hyperedges in  $H(X, S, k)$  is at most  $(2k - 1)|X| + O(k^2)$ . Moreover, this bound is tight up to an additive  $O(k^2)$  term. This refines a general result of Buzaglo, Pinchasi and Rote stating that every pseudodisc topological hypergraph with vertex set  $X$  has  $O(k^2|X|)$  hyperedges of size  $k$  or less. (Received July 17, 2014)