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**David J Hemmer\*** ([dhemmer@math.buffalo.edu](mailto:dhemmer@math.buffalo.edu)), 244 Math Building, Buffalo, NY 14260. *A Burnside-type theorem for faithful characters of the symmetric group.* Preliminary report.

Let  $G$  be a finite group and let  $U$  be a faithful irreducible representation of  $G$  over the complex numbers. In his 1911 book Burnside proved that every irreducible representation of  $G$  appears as a constituent of some tensor power of  $U$ . In 1964 Brauer refined the theorem by giving a specific  $d$  so each irreducible occurs inside one of  $\mathbb{C}, U, U^{\otimes 2}, \dots, U^{\otimes d}$ .

As the tensor algebra  $T(U)$  is infinite-dimensional, this theorem is perhaps not surprising. The exterior algebra  $\Lambda(U)$  has finite dimension  $2^{\dim U}$ , and Burnside's theorem does not hold for exterior powers.

We prove a strengthened exterior power version for the symmetric group  $\Sigma_n$ . The theorem is true only for  $n \geq 9$  and it is easy to see one must exclude the faithful irreducible given by the natural representation  $\chi^{(n-1,1)}$  and its twist by the sign representation. Then  $\Lambda^n(U)$  contains a free module, in particular contains every irreducible character. (Received July 28, 2014)