

1102-22-150

Hassan Lhou and **Jeb F. Willenbring*** (willenbring@gmail.com), University of Wisconsin - Milwaukee, Department of Mathematical Sciences, 3200 North Cramer Street, Milwaukee, WI 53211-3029. *Progress on a classification of small subgroups of a compact group*. Preliminary report.

Let \mathbb{G} be a connected reductive algebraic group, and let G be a real form, with a maximal compact subgroup K . Denote the Lie algebra of \mathbb{G} by \mathfrak{g} . To an irreducible, unitary G -representation, \mathcal{H} , one associates an underlying Harish-Chandra module \mathcal{M} for the pair (\mathfrak{g}, K) . The action of \mathfrak{g} on \mathcal{M} is irreducible, and K acts locally finitely. Furthermore, \mathcal{M} is *admissible* for K . That is, all irreps of K occur in \mathcal{M} with finite multiplicity. The classification of admissible Harish-Chandra modules is a major step toward finding the unitary dual of G .

This talk concerns the irreps of K and its subgroups. Given a closed subgroup S of K , every irrep of K can be regarded as a S -representation by restriction. We say that S is *small* in K if there exists $b > 0$ such that for all K -irreps, V , there exists an S -irrep, W , with dimension at most b and occurring in V . That is, the minimal dimension of an S -irrep occurring in a K -irrep is bounded by b .

One can ask, is \mathcal{M} admissible with respect to S ? A necessary condition for this to be true is that S is not small in K . We present results toward a classification of small subgroups of K . (Received July 27, 2014)