

1104-35-230

**Michael J Goldberg\*** (goldbem1@ucmail.uc.edu), Department of Mathematical Sciences, University of Cincinnati, Cincinnati, OH 45221-0025, and **William Green** (green@rose-hulman.edu), Department of Mathematics, Rose-Hulman Institute of Technology, TerreHaute, IN 47803. *Dispersive Estimates for Schrödinger Operators with a Threshold Eigenvalue.*

We prove dispersive estimates for the Schrödinger evolution  $e^{itH}P_{ac}(H)$  in  $\mathbb{R}^n$ ,  $n \geq 5$ , where  $H = -\Delta + V(x)$  has an eigenvalue at zero. As a map from  $L^1(\mathbb{R}^n)$  to  $L^\infty(\mathbb{R}^n)$  there is a rank one term decaying at the rate  $|t|^{2-\frac{n}{2}}$  and a finite rank operator with time decay  $|t|^{1-\frac{n}{2}}$ . The asymptotic expansion continues into more heavily weighted spaces; we show in particular that the remainder term after these finite rank pieces exists as a map from  $\langle x \rangle^{-2}L^1$  to  $\langle x \rangle^2L^\infty$ .

The initial finite rank terms both vanish if the eigenspace of  $H$  satisfies certain cancellation conditions, or equivalently if each eigenfunction satisfies the bound  $|\psi(x)| \leq C(1 + |x|)^{-n}$ . The extra cancellation also removes all need for weights when describing the behavior of the remaining evolution. Under those conditions we recover the same dispersive bound, mapping  $L^1(\mathbb{R}^n)$  to  $L^\infty(\mathbb{R}^n)$  with norm  $|t|^{-\frac{n}{2}}$ , as when zero is a regular point of the spectrum. (Received September 02, 2014)