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**Gregorio Chinni\*** ([chinni@ime.usp.br](mailto:chinni@ime.usp.br)), IME USP, Rua do Matão 1010, Butantã, São Paulo, SP, Brazil. *Perturbation of Globally Gevrey Hypoelliptic Operators.*

Let  $P(x, D)$  be a sum of squares analytic operator defined on the  $N$ -dimensional torus  $\mathbb{T}^N$  satisfying the Hörmander condition. It follows from a celebrated result of Hörmander [Acta Math. **119**, 1967, 147–171] that  $P(x, D)$  is locally subelliptic and hypoelliptic. By an easy global argument it then follows that there is an  $\epsilon > 0$  such that every solution to  $P(x, D) = f \in H^s(\mathbb{T}^N)$  belongs to  $H^{s+\epsilon}(\mathbb{T}^N)$ . The question we are dealing with is the following perturbation property: assume that  $P(x, D)$  as above is also globally Gevrey hypoelliptic of order  $s \geq 1$ . Is it true that  $P(x, D) + \Psi(x, D)$  is also globally Gevrey hypoelliptic of order  $s \geq 1$ , where  $\Psi(x, D)$  is an analytic pseudodifferential operator on  $\mathbb{T}^N$  of order  $< \epsilon$ ? In other words, can we assert that the subellipticity of  $P(x, D)$  is related with the order of perturbation that preserves the global Gevrey hypoelliptic of order  $s \geq 1$ ? We have the precise answer in the following cases: 1)  $P$  belongs to the class discussed in [Cordaro, P. and Himonas, A., Math.Res.Letters **1**, 1994, 501–510.] 2)  $P = P(D)$  is not necessarily in Hörmander class but has constant coefficients and is hypoelliptic as an operator in  $\mathbb{R}^N$ . (Received September 03, 2014)