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([mkoepp@math.ucdavis.edu](mailto:mkoepp@math.ucdavis.edu)) and **Michèle Vergne**. *Real multi-parameter Ehrhart theory:*

*Highest degree terms.*

We study sums  $S(P(b), h)$  of polynomials  $h$  over the lattice points in multi-parameter polytopes  $P(b) = \{Ax \leq b\}$ , where  $A$  is rational and  $b \in \mathbb{R}^N$  is a *real* parameter vector. On every chamber,  $S(P(b), h)$  is a generalized quasi-polynomial function of  $b$ , called the (weighted, real, multi-parameter) Ehrhart quasi-polynomial. It is a polynomial in variables  $b_i$  whose coefficients are periodic functions of the *real* parameters  $b_i$ . We give an algorithm for computing them in a certain closed form (“rational step-polynomials”).

This extends to the case of intermediate sums, which interpolate between integrals and discrete sums. Similar to Barvinok (2006), we show that certain linear combinations of the intermediate Ehrhart quasi-polynomials give an approximation of the Ehrhart quasi-polynomial. This gives an algorithm for computing the coefficients of the terms of the highest  $k$  degrees in variables  $b_i$ . In various interesting settings for varying dimension but fixed  $k$ , it runs in polynomial time.

The results are proved on the level of multi-parameter generating functions. We study their bidegree structure and approximation. (Received September 02, 2014)