We consider the spectra of three self-adjoint matrices associated with a combinatorial graph, viz., the adjacency matrix $A$, the graph Laplacian $H=-\Delta$, and the normalized graph Laplacian $L$. Using an averaged variational techniques we obtain sharp bounds on sums and the statistical distribution of the lowest k eigenvalues eigenvalues of these operators, and relate them to the structure of the graph. (Received February 04, 2014)

