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**Sergii M. Torba\*** ([storba@math.cinvestav.edu.mx](mailto:storba@math.cinvestav.edu.mx)). *On a new method of approximation of transmutation operators for Sturm-Liouville equations.*

An operator  $T$  is called a transmutation operator for the pair of operators  $A$  and  $B$  if it is continuous, continuously invertible on a suitable topological space and satisfy  $AT = TB$ .

When  $A = -\partial^2 + q(x)$  and  $B = -\partial^2$ , a transmutation operator  $T$  can be realized in the form

$$Tu(x) = u(x) + \int_{-x}^x K(x, t)u(t)dt$$

with the integral kernel  $K$  satisfying a Goursat problem. Due to the transmutation property the general solution of the equation  $Au = w^2u$  is a linear combination of the images of functions  $\cos wx$  and  $\sin wx/w$  under the action of  $T$ .

We propose a method of approximation of the integral kernel  $K(x, t)$  in the form of a polynomial in  $t$  whose coefficients are functions of  $x$ . Due to the form of the approximation all the integrals appearing during the calculation of  $T \sin wx$  and  $T \cos wx$  with the approximated kernel can be evaluated explicitly. The method starts from a particular solution  $f$  of the equation  $Af = 0$  and reduces the approximation of  $K$  to the solution of two one-dimensional approximation problems. All the steps of the method are suitable for numerical implementation leading to a highly efficient method of the solution of Sturm-Liouville spectral problems.

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